

1. Consider the following functions.

$$f(x) = 6x - 2$$

$$g(x) = 3x$$

$$h(x) = 2^x + 3$$

$$p(x) = 2$$

- a. Determine $(f + g)(x)$

$$9x - 2$$

- b. Determine $(f + h)(x)$

$$6x + 2^x + 1$$

- c. Determine $(g - f)(x)$

$$-3x + 2$$

- d. Determine $(p \cdot g)(x)$

$$6x$$

- e. Determine $(f \cdot g)(2)$

$$60$$

- f. Determine $\left(\frac{f}{g}\right)(x)$

$$2 - \frac{2}{3x}$$

2. Given the following partial set of values of function evaluate the following.

x	-1	0	1	2	3
$f(x)$	1	2	4	8	16
$g(x)$	-5	-3	-1	1	3

- a. Determine $f(1) - 2 \cdot g(2)$

$$4 - (2)(1) = 2$$

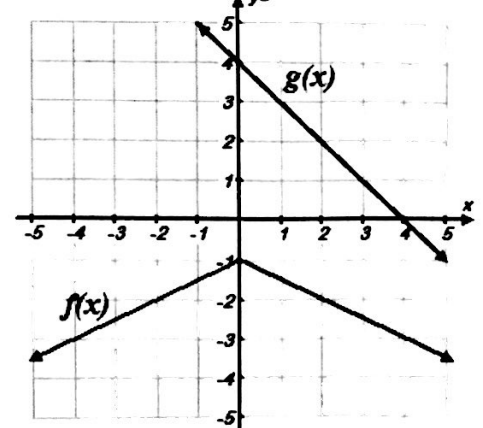
- b. Determine $(f + g)(2)$

$$f(2) + g(2) = 8 + 1 = 9$$

3. Given the following partial set of values of function evaluate the following.

- a. Determine $f(4) + 2 \cdot g(1)$

$$-3 + (2)(3) = 3$$



4. Consider the following functions.

$$f(x) = 6x - 2$$

$$g(x) = 3x$$

$$h(x) = 2^x + 3$$

$$p(x) = 2$$

a. Determine $(f \circ h)(1)$

$$\begin{aligned} &= f(h(1)) \\ &= f(5) \\ &= 28 \end{aligned}$$

b. Determine $(g \circ f)(2)$

$$\begin{aligned} &= g(f(x)) \\ &= g(10) \\ &= 30 \end{aligned}$$

c. Determine $(f \circ g)(x)$

$$\begin{aligned} &f(g(x)) \\ &= 6(3x) - 2 \\ &= 18x - 2 \end{aligned}$$

d. Determine $(g \circ h)(x)$

$$\begin{aligned} &g(h(x)) \\ &= 3(2^x + 3) \\ &= 3 \cdot 2^x + 9 \end{aligned}$$

5. Given the following partial set of values of function evaluate the following.

x	-1	0	1	2	3
$f(x)$	1	2	4	8	16
$g(x)$	-5	-3	-1	1	3

a. Determine $(f \circ g)(2)$

$$\begin{aligned} f(g(2)) &= f(1) \\ &= 4 \end{aligned}$$

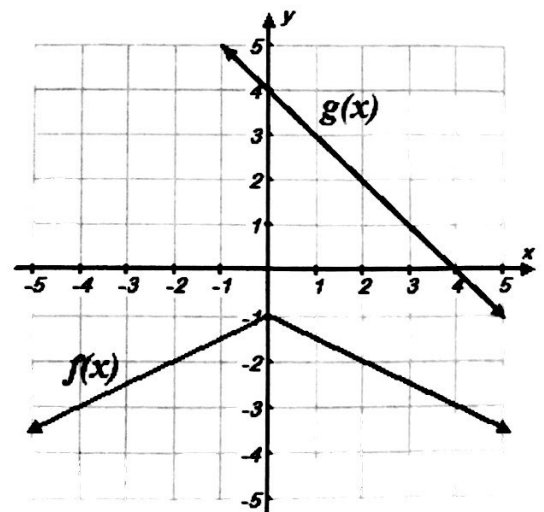
b. Determine $(g \circ f)(0)$

$$g(f(0)) = g(2) = 1$$

6. Given the following partial set of values of function evaluate the following.

a. Determine $(f \circ g)(0)$

$$\begin{aligned} &= f(g(0)) \\ &= f(4) \\ &= -3 \end{aligned}$$



7. The **length** of a rectangle can be described by the function $f(x) = 6x - 2$ and the **width** of the same rectangle can be described by $g(x) = 2x + 1$



a. Determine $(f \cdot g)(x)$ and explain what it represents.

$$(6x-2)(2x+1) = 12x^2 + 2x - 2$$

This function represents the area of the rectangle.

b. Determine an expression that represents the perimeter of the rectangle.

$$2(6x-2) + 2(2x+1)$$

$$= 12x - 4 + 4x + 2 = 16x - 2$$

8. Simplify each composition completely.

Given: $f(x) = 10 - x^2$

$$g(x) = \frac{3}{x+1}$$

$$h(x) = x - 3$$

a. $f(h(x))$

$$= 10 - (x-3)^2$$

$$= 10 - (x^2 - 6x + 9)$$

$$= -x^2 + 6x + 1$$

b. $g(h(f(x)))$

$$g(10 - x^2 - 3) = g(7 - x^2)$$

$$= \frac{3}{7 - x^2 + 1} = \frac{3}{8 - x^2}$$

9. Verify which of the following are inverses of one another by considering $f(g(x))$ and $g(f(x))$

$$f(x) = 4x$$

a. $g(x) = \frac{x}{4}$

$$f(g(x)) = 4\left(\frac{x}{4}\right)$$

$$= x$$

They are inverses

$$g(f(x)) = \frac{4x}{4}$$

$$= x$$

$$f(x) = 2x + 1$$

b. $g(x) = \frac{x-1}{2}$

$$f(g(x)) = 2\left(\frac{x-1}{2}\right) + 1$$

$$= x - 1 + 1$$

$$= x$$

They are inverses

$$g(f(x)) = \frac{2x+1-1}{2}$$

$$= \frac{2x}{2}$$

$$= x$$

c. $f(x) = \frac{x}{2} - 3$

$$g(x) = 2x + 3$$

$$f(g(x)) = \frac{2x+3}{2} - 3$$

$$= \frac{2x+3}{2} - 3$$

$$= \frac{2x}{2} + \frac{3}{2} - 3$$

$$= x - \frac{3}{2}$$

They are not inverses

$$g(f(x)) = 2\left(\frac{x}{2} - 3\right) + 3$$

$$f(g(x)) = 2\left(\sqrt[3]{\frac{x+1}{2}}\right)^3 - 1$$

$$= 2\left(\frac{x+1}{2}\right)^3 - 1$$

$$= x + 1 - 1$$

$$= x$$

They are inverses

$$g(f(x)) = \sqrt[3]{\frac{2x^3-1}{2}} + 1$$

$$= \sqrt[3]{\frac{2x^3-1}{2}} + 1$$

$$= \sqrt[3]{2x^3-1} + 1$$

$$= x$$

10. Find the inverse relation.

a. $f(x) = \frac{(x-2)^6}{5} - 9$

$x = \frac{(y-2)^6}{5} - 9$

$\sqrt[6]{5(x+9)} = \sqrt[6]{(y-2)^6}$
 $\sqrt[6]{5(x+9)} + 2 = y$

b. $g(x) = \frac{4}{5-x^3}$

$(5-y^3)x = \frac{4}{5-y^3} \cdot (5-y^3)$
 $(5-y^3)(x) = \frac{4}{x}$

$5-y^3 = \frac{4}{x}$
 $-y^3 = \frac{4}{x} - 5$
 $y^3 = -\frac{4}{x} + 5$
 $y = \sqrt[3]{-\frac{4}{x} + 5}$

11. The shoe size for the average U.S. teen or adult male can be modeled by the function $M(x) = 3x-22$ where x is the length of the foot in inches.

a. Find the inverse of the function above.

$x = 3y - 22$

$\frac{x+22}{3} = y$

b. Explain in words what the inverse function represents.

The inverse function will give you someone's foot length given their shoe size

12. Divide using long division.

a. $(9x^4 + 30x^3 - 15x - 9) \div (x^2 + 3x)$

$$\begin{array}{r} 9x^2 + 3x - 9 + \frac{12x-9}{x^2+3x} \\ x^2+3x+0 \overline{) 9x^4+30x^3+0x^2-15x-9} \\ \underline{-(9x^4+27x^3+0x^2)} \\ 3x^3+0x^2-15x \\ \underline{-(3x^3+9x^2+0x)} \\ -9x^2-15x-9 \\ \underline{-(-9x^2-27x-0)} \\ 12x-9 \end{array}$$

b. $(3x^3 - 17x^2 + 21x + 25) \div (x^2 - 2x - 3)$

$$\begin{array}{r} 3x - 11 + \frac{8x-8}{x^2-2x-3} \\ x^2-2x-3 \overline{) 3x^3-17x^2+21x+25} \\ \underline{-(3x^3-6x^2-9x)} \\ -11x^2+30x+25 \\ \underline{-(-11x^2+22x+33)} \\ 8x-8 \end{array}$$

13. Divide using synthetic division.

a. $(x^4 - 9x^3 + 16x^2 + 8x + 18) \div (x - 6)$

$$\begin{array}{r|rrrrrr} 6 & 1 & -9 & 16 & 8 & 18 \\ & & 6 & -18 & -12 & -24 \\ \hline & 1 & -3 & -2 & -4 & -6 \end{array}$$

 $x^3 - 3x^2 - 2x - 4 - \frac{6}{x-6}$

b. $(7x^4 - 6x^2 + 6x - 5) \div (x + 1)$

$$\begin{array}{r|rrrrr} -1 & 7 & 0 & -6 & 6 & -5 \\ & & -7 & 7 & -1 & -5 \\ \hline & 7 & -7 & 1 & 5 & -10 \end{array}$$

 $7x^3 - 7x^2 + x - 5 - \frac{10}{x+1}$

14. Factor completely.

a. $2x^3 + 16$

$2(x^3 + 8) = 2(x^3 + 2^3)$
 $= 2(x+2)(x^2 - 2x + 4)$

b. $27x^3 - 64 = (3x)^3 - (4)^3$

$= (3x-4)(9x^2 + 12x + 16)$