

Sum & Diff Identities Practice

Date _____ Period _____

Find the exact value of each. For the first four, condense first.

1) $\cos 126\cos 9 - \sin 126\sin 9$

2) $\sin \frac{5\pi}{9}\cos \frac{2\pi}{9} - \cos \frac{5\pi}{9}\sin \frac{2\pi}{9}$

3)
$$\frac{\tan \frac{16\pi}{9} - \tan \frac{19\pi}{36}}{1 + \tan \frac{16\pi}{9}\tan \frac{19\pi}{36}}$$

4) $\sin 220\cos 85 - \cos 220\sin 85$

5) $\tan \frac{7\pi}{12}$

6) $\cos \frac{19\pi}{12}$

7) $\cos 75$

8) $\tan 105$

Simplify/Condense.

9) $\cos 5x \cos -6x - \sin 5x \sin -6x$

10) $\cos -2v \cos -2v - \sin -2v \sin -2v$

11) $\frac{\tan -2v - \tan -3v}{1 + \tan -2v \tan -3v}$

12) $\cos 2x \cos -3x + \sin 2x \sin -3x$

Verify each identity.

13) $\sin (180 - \theta) = \sin \theta$

14) $\cos \left(\frac{\pi}{2} + \theta \right) = -\sin \theta$

15) $\sin \left(\theta - \frac{3\pi}{2} \right) = \cos \theta$

16) $\tan \left(\frac{\pi}{4} - \theta \right) = \frac{1 - \tan \theta}{1 + \tan \theta}$

Answers to Sum & Diff Identities Practice

$$1) -\frac{\sqrt{2}}{2}$$

$$5) -2 - \sqrt{3}$$

$$9) \cos -x$$

$$\begin{aligned} 13) \sin(180 - \theta) &= \sin 180 \cos \theta - \cos 180 \sin \theta \\ &= 0 \cos \theta - (-1) \sin \theta \\ &= \sin \theta \end{aligned}$$

$$\begin{aligned} 16) \tan\left(\frac{\pi}{4} - \theta\right) &= \frac{\tan \frac{\pi}{4} - \tan \theta}{1 + \tan \frac{\pi}{4} \tan \theta} \\ &= \frac{1 - \tan \theta}{1 + \tan \theta} \\ &= \frac{1 - \tan \theta}{1 + \tan \theta} \end{aligned}$$

$$2) \frac{\sqrt{3}}{2}$$

$$6) \frac{\sqrt{6} - \sqrt{2}}{4}$$

$$10) \cos -4v$$

$$\begin{aligned} 14) \cos\left(\frac{\pi}{2} + \theta\right) &= \cos \frac{\pi}{2} \cos \theta - \sin \frac{\pi}{2} \sin \theta \\ &= 0 \cos \theta - \sin \theta \\ &= -\sin \theta \end{aligned}$$

$$3) 1$$

$$7) \frac{\sqrt{6} - \sqrt{2}}{4}$$

$$11) \tan v$$

$$4) \frac{\sqrt{2}}{2}$$

$$8) -2 - \sqrt{3}$$

$$12) \cos 5x$$

$$\begin{aligned} 15) \sin\left(\theta - \frac{3\pi}{2}\right) &= \sin \theta \cos \frac{3\pi}{2} - \cos \theta \sin \frac{3\pi}{2} \\ &= \sin \theta \cdot 0 - \cos \theta \cdot (-1) \\ &= \cos \theta \end{aligned}$$