

Sum/Diff Identities Practice

Date _____ Period _____

Simplify.

1) $\sin 6u \cos -u + \cos 6u \sin -u$

2) $\frac{\tan 4v + \tan 3v}{1 - \tan 4v \tan 3v}$

3) $\sin 6x \cos 5x + \cos 6x \sin 5x$

4) $\cos \theta \cos -3\theta - \sin \theta \sin -3\theta$

5) $\sin -2\theta \cos -6\theta + \cos -2\theta \sin -6\theta$

6) $\sin 5\theta \cos 3\theta - \cos 5\theta \sin 3\theta$

7) $\sin -3u \cos 5u + \cos -3u \sin 5u$

8) $\cos -2\theta \cos -4\theta + \sin -2\theta \sin -4\theta$

Verify each identity.

9) $\cos\left(\frac{\pi}{2} + \theta\right) = -\sin \theta$

10) $\cos\left(\theta - \frac{3\pi}{2}\right) = -\sin \theta$

11) $\tan\left(\frac{\pi}{4} + \theta\right) = \frac{1 + \tan \theta}{1 - \tan \theta}$

12) $\sin(\theta + \pi) = -\sin \theta$

13) $\tan(\theta + 180) = \tan \theta$

14) $\sin(90 + \theta) = \cos \theta$

Answers to Sum/Diff Identities Practice

1) $\sin 5u$

5) $\sin -8\theta$

9) $\cos\left(\frac{\pi}{2} + \theta\right)$
 $= \cos \frac{\pi}{2} \cos \theta - \sin \frac{\pi}{2} \sin \theta$
 $= 0 \cos \theta - \sin \theta$
 $= -\sin \theta$

12) $\sin(\theta + \pi)$

$$\begin{aligned} &= \sin \theta \cos \pi + \cos \theta \sin \pi \\ &= \sin \theta \cdot -1 + \cos \theta \cdot 0 \\ &= -\sin \theta \end{aligned}$$

2) $\tan 7v$

6) $\sin 2\theta$

10) $\cos\left(\theta - \frac{3\pi}{2}\right)$
 $= \cos \theta \cos \frac{3\pi}{2} + \sin \theta \sin \frac{3\pi}{2}$
 $= \cos \theta \cdot 0 + \sin \theta \cdot -1$
 $= -\sin \theta$

13) $\tan(\theta + 180)$

$$\begin{aligned} &= \frac{\tan \theta + \tan 180}{1 - \tan \theta \tan 180} \\ &= \frac{\tan \theta + 0}{1 - \tan \theta \cdot 0} \\ &= \tan \theta \end{aligned}$$

3) $\sin 11x$

7) $\sin 2u$

4) $\cos -2\theta$

8) $\cos 2\theta$

11) $\tan\left(\frac{\pi}{4} + \theta\right)$
 $= \frac{\tan \frac{\pi}{4} + \tan \theta}{1 - \tan \frac{\pi}{4} \tan \theta}$
 $= \frac{1 + \tan \theta}{1 - \tan \theta}$
 $= \frac{1 + \tan \theta}{1 - \tan \theta}$

14) $\sin(90 + \theta)$

$$\begin{aligned} &= \sin 90 \cos \theta + \cos 90 \sin \theta \\ &= \cos \theta + 0 \sin \theta \\ &= \cos \theta \end{aligned}$$