

# Function Composition Practice Problems

Name \_\_\_\_\_

Key

Period \_\_\_\_\_

Date \_\_\_\_\_

$$f(x) = 3x + 2; \quad g(x) = 4x - 1$$

1.  $f(g(x))$

$$\begin{aligned} &3(4x-1) + 2 \\ &12x - 3 + 2 \\ &\boxed{12x - 1} \end{aligned}$$

2.  $g(f(x))$

$$\begin{aligned} &4(3x+2) - 1 \\ &12x + 8 - 1 \\ &\boxed{12x + 7} \end{aligned}$$

3.  $f(g(2))$

$$3(2(2) - 1) - 1 = \boxed{23}$$

$$f(x) = x^2; \quad g(x) = 2x - 5$$

4.  $f(g(x))$

$$\begin{aligned} &(2x-5)^2 \\ &(2x-5)(2x-5) \\ &\boxed{4x^2 - 20x + 25} \end{aligned}$$

5.  $g(f(x))$

$$\begin{aligned} &2(x^2) - 5 \\ &\boxed{2x^2 - 5} \end{aligned}$$

6.  $g(f(2))$

$$\begin{aligned} &2(2)^2 - 5 \\ &8 - 5 \\ &\boxed{3} \end{aligned}$$

$$f(x) = 2x^2 - 4x; \quad g(x) = x^2$$

7.  $f(g(x))$

$$\begin{aligned} &2(x^2)^2 - 4(x^2) \\ &\boxed{2x^4 - 4x^2} \end{aligned}$$

8.  $g(f(x))$

$$\begin{aligned} &(2x^2 - 4x)^2 \\ &(2x^2 - 4x)(2x^2 - 4x) \\ &\boxed{4x^4 - 16x^3 + 16x^2} \end{aligned}$$

9.  $f(g(2))$

$$\begin{aligned} &2(2)^4 - 4(2)^2 \\ &32 - 16 \\ &\boxed{16} \end{aligned}$$

$$f(x) = 3x - 4; \quad g(x) = (x - 1)^2; \quad h(x) = 4x$$

10.  $h(g(f(x)))$

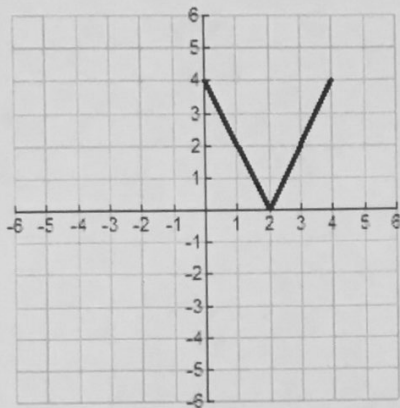
$$\begin{aligned} &4(3x-4-1)^2 \\ &4(3x-5)^2 \\ &4(3x-5)(3x-5) \\ &4(9x^2 - 30x + 25) = \boxed{36x^2 - 120x + 100} \end{aligned}$$

11.  $g(h(f(x)))$

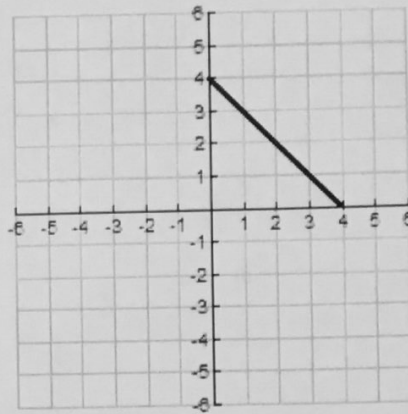
$$\begin{aligned} &(4(3x-4) - 1)^2 \\ &(12x - 16 - 1)^2 \\ &(12x - 17)^2 \\ &(12x - 17)(12x - 17) \\ &\boxed{144x^2 - 408x + 289} \end{aligned}$$

Use the graphs of  $f$  and  $g$  to evaluate the functions.

$$y = f(x)$$



$$y = g(x)$$



12.  $(f+g)(3)$   
 $f(3) + g(3)$   
 $2 + 1$   
 $= \boxed{3}$

13.  $(f/g)(2)$   
 $\frac{f(2)}{g(2)} = \frac{0}{2} = \boxed{0}$

14.  $(f-g)(1)$   
 $f(1) - g(1)$   
 $2 - 3 = \boxed{-1}$

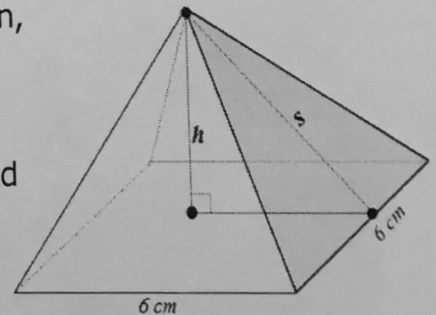
15.  $(fg)(4)$   
 $f(4) \cdot g(4)$   
 $(4)(0) = \boxed{0}$

16.  $(fo g)(2)$   
 $f(g(2))$   
 $= f(0)$   
 $= \boxed{4}$

17.  $(go f)(3)$   
 $g(f(3))$   
 $= g(2)$   
 $= \boxed{0}$

18. A pyramid is created from a square base where each side is 6 cm. The volume of the pyramid can be given by the function,  $V(h) = 12h$ .

The function to calculate the height of the same square based pyramid given the slant height could be described by  $H(s) = \sqrt{s^2 - 9}$  where 's' is the slant height in cm.



a. Evaluate  $V(H(5))$

$$12 (\sqrt{5^2 - 9})$$

$$= \boxed{48 \text{ cm}^3}$$

b. Explain what  $V(H(5))$  represent

The volume of the square pyramid when the slant height is known to be 5 cm.